

DIAGRAM FOR
REINFORCED
CONCRETE.



LIST OF SYMBOLS

- A Area.
- A Total cross-sectional area of a pillar.
- A_1 Area of concrete.
- A_L Cross-sectional area of longitudinal steel rods in a pillar.
- A_H Cross-sectional area of a hooped reinforcing rod in a pillar.
- A_E Equivalent area.
- A_c Area of compressive reinforcement in beams.
- A_T Area of tensile reinforcement in beams.
- A_s Area of shear reinforcement.
- A_t Total area.
- a Buckling factor of a column.
-
- B_b Ratio I/l for beams, i.e. a measure of stiffness.
- B_c Ratio I/l for column.
- b Breadth.
- b Breadth of rectangular beam.
- b_r Breadth of the rib in a T-beam.
- b_s Effective breadth of the slab in a T-beam.
-
- C Total compressive force or stress.

- C_c Total compression on concrete.
 C_s Total compression on steel.
 e Compressive stress intensity.
 c Compressive stress intensity on concrete.
 C_p Compressive stress in column not hooped.
 C' Minimum compressive stress in concrete for combined bending and direct load.
 C_s Compressive stress intensity on steel.
 C_r Ratio C_s/e .
 C_s' Minimum compressive stress in steel for combined bending and direct load.
 C^l Compressive stress intensity in long column.
 d Depth.
 d Effective depth of a beam from top of a beam to axis of tensile reinforcement.
 d_s Total depth of a slab in a T-beam.
 d_c Depth or distance of the centre of compressive reinforcement from the compressed edge.
 d' Distance of the centre of reinforcement from any edge.
 d Any diameter.
 d Outside diameter.
 d_i Insid diameter.

d_k	<u>Diameter</u> of the core of a pillar with hooped reinforcement.
d_l	<u>Diameter</u> of a <u>longitudinal</u> reinforcing rod of a pillar.
d_h	<u>Diameter</u> of a <u>herical</u> reinforcing rod of a pillar.
d_b	<u>Diameter</u> of stirrup bar.
E	<u>Elastic</u> modulus of any materials.
E_c	<u>Elastic</u> modulus of <u>concrete</u> in compression.
E_s	<u>Elastic</u> modulus of steel.
e	<u>Eccentricity</u> of any load.
e_c	Unit <u>elongation</u> of <u>concrete</u> .
e_s	Unit <u>elongation</u> of <u>steel</u> .
F	Total <u>friction</u> between any two surfaces.
f	<u>Friction</u> or adhesion between surfaces in unit of force per unit of area.
f	Intensity of stress (general)
f	<u>Fiber</u> stress intensity.
f_c	<u>Compressive</u> stress intensity.
f_t	<u>Tensile</u> stress intensity.
f_b	<u>Bearing</u> stress intensity.
f_u	Intensity of <u>ultimate</u> stress.
g	<u>Gravity</u> .

H	<u>Horizontal</u> component of force.
h	Intensity of <u>horizontal</u> shearing stress.
h	Any height.
h	Total <u>height</u> of beam.
I	<u>Inertia</u> moment.
I _x	<u>Inertia</u> moment on axis XX.
I _y	<u>Inertia</u> moment on axis YY.
I _s	<u>Inertia</u> moment for <u>steel</u> .
I _c	<u>Inertia</u> moment for <u>concrete</u> .
I _e	<u>Inertia</u> moment for <u>equivalent</u> section.
I _n	<u>Inertia</u> moment on <u>neutral axis</u> .
I _g	<u>Inertia</u> moment on <u>gravity axis</u> .
i	Radius of gyration.
j	Arm of any couple, i.e. distance between two parallel force of equal magnitude, but acting in opposite directions.
j	Arm of the couple formed by the compressive and tensile forces in beam.
j ₁	Ratio j/d .
K	A constant.

TABLE I	FORMULÆ FOR RECTANGULAR BEAM.					
	r	$\frac{A_r}{bd}$	$\frac{m}{2t_1(t_1+m)}$	1		
	t_1	$\frac{t}{c}$	$\frac{m}{2}(\sqrt{1+\frac{2}{mr}}-1)$	1'		
	k	k_1d	$\frac{m}{t_1+m} \cdot d$	2		
			$mr(\sqrt{1+\frac{2}{mr}}-1) \cdot d$	2'		
	u	u_1d	$\frac{k_1}{3} \cdot d$	3		
			$\frac{m}{3}(\sqrt{1+\frac{2}{mr}}-1) \cdot d$	3'		
	j	j_1d	$(1-u_1) \cdot d$	4		
			$(1-\frac{k_1}{3}) \cdot d$	$\frac{3t_1+2m}{3(t_1+m)} \cdot d$ $\{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)\} \cdot d$	4'	
	A_r	rbd	$\frac{1}{j_1t} \cdot \frac{M}{d}$	5		
			$\frac{1}{(1-\frac{k_1}{3})t} \cdot \frac{M}{d}$	5'		
			$\frac{1}{t_1j_1c} \cdot \frac{M}{d}$	$\frac{3(t_1+m)}{(3t_1+2m)t} \cdot \frac{M}{d}$ $\frac{1}{\{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)\}t} \cdot \frac{M}{d}$	6	
			$\frac{1}{t_1(1-\frac{k_1}{3})c} \cdot \frac{M}{d}$	$\frac{3(t_1+m)}{t_1(3t_1+2m)c} \cdot \frac{M}{d}$ $\frac{1}{t_1\{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)\}c} \cdot \frac{M}{d}$	6'	
	d	$\sqrt{\frac{M}{N_1b}}$	$\sqrt{\frac{1}{rj_1t} \cdot \frac{M}{b}}$	7		
			$\sqrt{\frac{1}{r(1-\frac{k_1}{3})t} \cdot \frac{M}{b}}$	$\sqrt{\frac{6t_1(t_1+m)^2}{m(3t_1+2m)t} \cdot \frac{M}{b}}$	8	
			$\sqrt{\frac{2}{k_1j_1c} \cdot \frac{M}{b}}$	8		
			$\sqrt{\frac{2}{k_1(1-\frac{k_1}{3})c} \cdot \frac{M}{b}}$			
	b	$\frac{M}{N_1d^2}$	$\frac{1}{rj_1t} \cdot \frac{M}{d^2}$	9		
			$\frac{1}{r(1-\frac{k_1}{3})t} \cdot \frac{M}{d^2}$	$\frac{6t_1(t_1+m)^2}{m(3t_1+2m)t} \cdot \frac{M}{d^2}$	10	
			$\frac{2}{k_1j_1c} \cdot \frac{M}{d^2}$	10		
			$\frac{2}{k_1(1-\frac{k_1}{3})c} \cdot \frac{M}{d^2}$			
	d	$\sqrt[3]{\frac{M}{N_1\eta}}$	$\sqrt[3]{\frac{1}{rj_1t} \cdot \frac{M}{\eta}}$	11		
			$\sqrt[3]{\frac{1}{r(1-\frac{k_1}{3})t} \cdot \frac{M}{\eta}}$	$\sqrt[3]{\frac{6(t_1+m)^2}{m(3t_1+2m)c} \cdot \frac{M}{\eta}}$	12	
			$\sqrt[3]{\frac{2}{k_1j_1c} \cdot \frac{M}{\eta}}$	12		
			$\sqrt[3]{\frac{2}{k_1(1-\frac{k_1}{3})c} \cdot \frac{M}{\eta}}$			
	t	t_1c	$\frac{1}{rj_1} \cdot \frac{M}{bd^2}$	13		
			$\frac{1}{r(1-\frac{k_1}{3})} \cdot \frac{M}{bd^2}$	13		
	c	$\frac{t}{t_1}$	$\frac{2}{k_1j_1} \cdot \frac{M}{bd^2}$	14		
			$\frac{2}{k_1(1-\frac{k_1}{3})} \cdot \frac{M}{bd^2}$	14		
	$\frac{T}{C}$	$\frac{M}{j}$	$\frac{1}{j_1} \cdot \frac{M}{d}$	15		
			$\frac{1}{(1-\frac{k_1}{3})} \cdot \frac{M}{d}$	$\frac{3(t_1+m)}{3t_1+2m} \cdot \frac{M}{d}$ $\frac{1}{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)} \cdot \frac{M}{d}$	15'	
	M	T_j	$rj_1t \cdot bd^2$	16		
			$r(1-\frac{k_1}{3})t \cdot bd^2$	$\frac{3t_1+2m}{6t_1(t_1+m)^2} m \cdot t \cdot bd^2$	16	
		C_j	$\frac{1}{2}k_1j_1c \cdot bd^2$	17		
			$\frac{k_1}{2}(1-\frac{k_1}{3})c \cdot bd^2$	17		

a

b

TABLE I	FORMULÆ FOR RECTANGULAR BEAM.					
	Section	Strain diagram	Stress diagram			
r	$\frac{A_r}{bd}$	$\frac{m}{2t_1(t_1+m)}$			1	
t ₁	$\frac{t}{c}$	$\frac{m}{2} \cdot (\sqrt{1 + \frac{2}{mr}} - 1)$			1'	
k	k ₁ d	$\frac{m}{t_1+m} \cdot d$			2	
		$mr(\sqrt{1 + \frac{2}{mr}} - 1) \cdot d$			2'	
u	u ₁ d	$\frac{k_1}{3} \cdot d$			3	
		$\frac{m}{3(t_1+m)} \cdot d$			3'	
j	j ₁ d	$(1-u_1) \cdot d$	$(1 - \frac{k_1}{3}) \cdot d$	$\frac{3t_1+2m}{3(t_1+m)} \cdot d$	4	
				$\{1 - \frac{mr}{3}(\sqrt{1 + \frac{2}{mr}} - 1)\} \cdot d$	4'	
A _r	rbd	$\frac{1}{j_1 t} \cdot \frac{M}{d}$	$\frac{1}{(1 - \frac{k_1}{3}) \cdot t} \cdot \frac{M}{d}$	$\frac{3(t_1+m)}{(3t_1+2m) \cdot t} \cdot \frac{M}{d}$	5	
				$\frac{1}{\{1 - \frac{mr}{3}(\sqrt{1 + \frac{2}{mr}} - 1)\} \cdot t} \cdot \frac{M}{d}$	5'	
		$\frac{1}{t_1 j_1 \cdot c} \cdot \frac{M}{d}$	$\frac{1}{t(1 - \frac{k_1}{3}) \cdot c} \cdot \frac{M}{d}$	$\frac{3(t_1+m)}{t_1(3t_1+2m) \cdot c} \cdot \frac{M}{d}$	6	
				$\frac{1}{t_1 \{1 - \frac{mr}{3}(\sqrt{1 + \frac{2}{mr}} - 1)\} \cdot c} \cdot \frac{M}{d}$	6'	
d	$\sqrt{\frac{M}{N_1 b}}$	$\sqrt{\frac{1}{r j_1 \cdot t} \cdot \frac{M}{b}}$	$\sqrt{\frac{1}{r(1 - \frac{k_1}{3}) \cdot t} \cdot \frac{M}{b}}$	$\sqrt{\frac{6t_1(t_1+m)^2}{m(3t_1+2m) \cdot t} \cdot \frac{M}{b}}$	7	
		$\sqrt{\frac{2}{k_1 j_1 \cdot c} \cdot \frac{M}{b}}$	$\sqrt{\frac{2}{k_1(1 - \frac{k_1}{3}) \cdot c} \cdot \frac{M}{b}}$	$\sqrt{\frac{6(t_1+m)^2}{m(3t_1+2m) \cdot c} \cdot \frac{M}{b}}$	8	
b	$\frac{M}{N_1 d^2}$	$\frac{1}{r j_1 \cdot t} \cdot \frac{M}{d^2}$	$\frac{1}{r(1 - \frac{k_1}{3}) \cdot t} \cdot \frac{M}{d^2}$	$\frac{6t_1(t_1+m)^2}{m(3t_1+2m) \cdot t} \cdot \frac{M}{d^2}$	9	
		$\frac{2}{k_1 j_1 \cdot c} \cdot \frac{M}{d^2}$	$\frac{2}{k_1(1 - \frac{k_1}{3}) \cdot c} \cdot \frac{M}{d^2}$	$\frac{6(t_1+m)^2}{m(3t_1+2m) \cdot c} \cdot \frac{M}{d^2}$	10	
$(\frac{b}{d} = \eta)$ d	$\sqrt[3]{\frac{M}{N_1 \eta}}$	$\sqrt[3]{\frac{1}{r j_1 \cdot t} \cdot \frac{M}{\eta}}$	$\sqrt[3]{\frac{1}{r(1 - \frac{k_1}{3}) \cdot t} \cdot \frac{M}{\eta}}$	$\sqrt[3]{\frac{6t_1(t_1+m)^2}{m(3t_1+2m) \cdot t} \cdot \frac{M}{\eta}}$	11	
		$\sqrt[3]{\frac{2}{k_1 j_1 \cdot c} \cdot \frac{M}{\eta}}$	$\sqrt[3]{\frac{2}{k_1(1 - \frac{k_1}{3}) \cdot c} \cdot \frac{M}{\eta}}$	$\sqrt[3]{\frac{6(t_1+m)^2}{m(3t_1+2m) \cdot c} \cdot \frac{M}{\eta}}$	12	
t	t ₁ c	$\frac{1}{r j_1} \cdot \frac{M}{bd^2}$	$\frac{1}{r(1 - \frac{k_1}{3})} \cdot \frac{M}{bd^2}$	$\frac{3}{mr^2(2 - \sqrt{1 + \frac{2}{mr}})} \cdot \frac{M}{bd^2}$	13	
c	$\frac{t}{t_1}$	$\frac{2}{k_1 j_1} \cdot \frac{M}{bd^2}$	$\frac{2}{k_1(1 - \frac{k_1}{3})} \cdot \frac{M}{bd^2}$	$\frac{3(\sqrt{1 + \frac{2}{mr}} - 1)}{2r^2(2 - \sqrt{1 + \frac{2}{mr}})} \cdot \frac{M}{bd^2}$	14	
$\frac{T}{C}$	$\frac{M}{j}$	$\frac{1}{j_1} \cdot \frac{M}{d}$	$\frac{1}{(1 - \frac{k_1}{3})} \cdot \frac{M}{d}$	$\frac{3(t_1+m)}{3t_1+2m} \cdot \frac{M}{d}$	15	
				$\frac{1}{1 - \frac{mr}{3}(\sqrt{1 + \frac{2}{mr}} - 1)} \cdot \frac{M}{d}$	15'	
M	T _j	$r j_1 \cdot t \cdot bd^2$	$r(1 - \frac{k_1}{3}) \cdot t \cdot bd^2$	$\frac{3t_1+2m}{6t_1(t_1+m)^2} m \cdot t \cdot bd^2$	16	
	C _j	$\frac{1}{2} k_1 j_1 \cdot c \cdot bd^2$	$\{\frac{k_1}{2}(1 - \frac{k_1}{3})\} \cdot c \cdot bd^2$	$\frac{3t_1+2m}{6(t_1+m)^2} m \cdot c \cdot bd^2$	17	

a

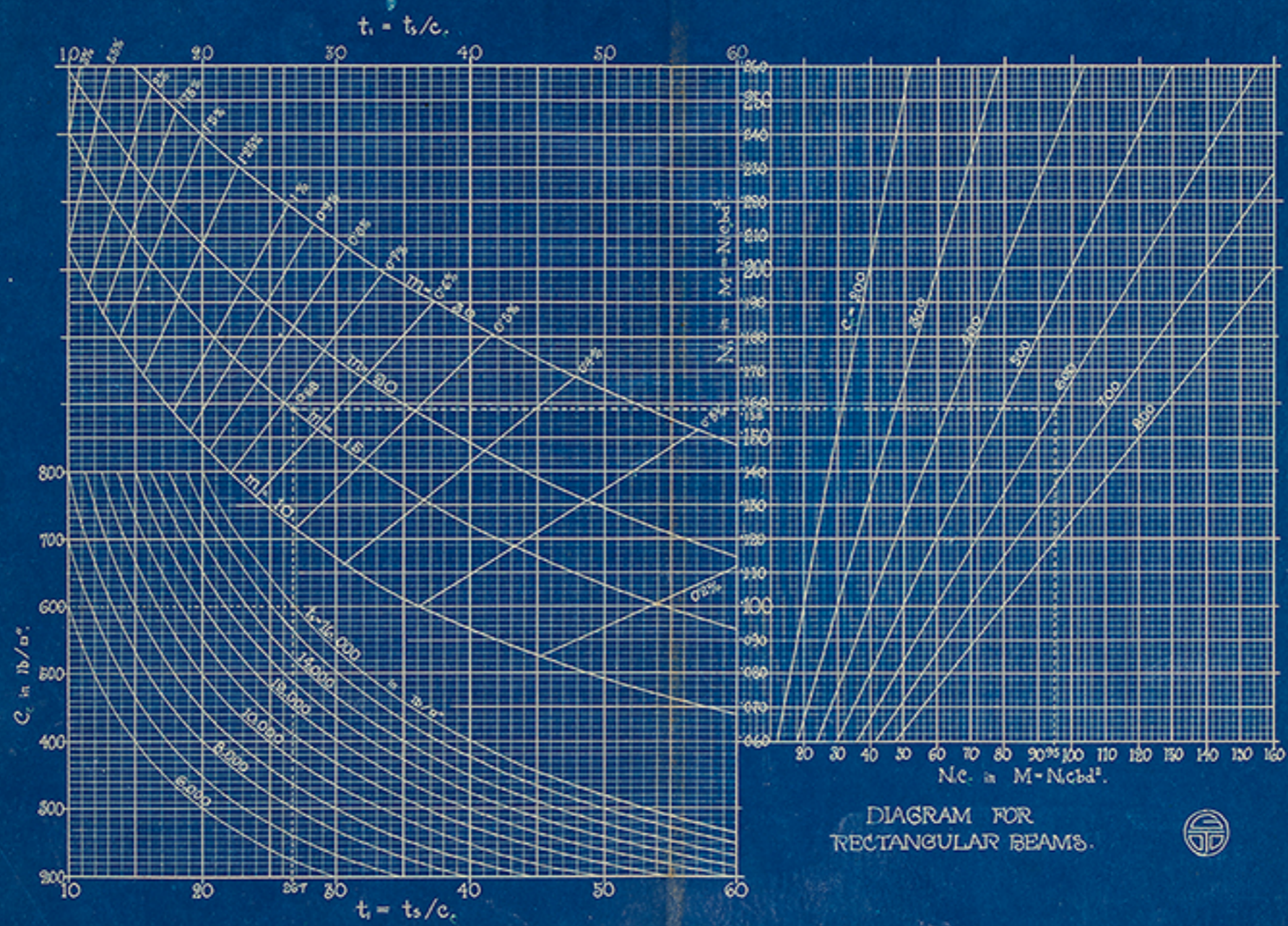
b

The Beam and its Load with the B.M. and S.F. Diagrams.	B.M. Equation and Maximum B.M. M_x & M	Equation of Elastic Line, & Max. Deflection in Terms of The Loading. y & Δ	Max. Deflection in Terms of Stress on Extreme Fiber of Symmetrical Section. Δ_f	Max. Stress on Extreme Fiber in Terms of the Loading Symmetrical Section. f .	Breaking Weight in Terms of the Pure Stress P	S.F. Equation, Max. S.F. and Reactions. S_x , S_a & R_b	Relative Strength
	$M_x = \frac{Px}{2}(l-x)$ $M_{\frac{1}{2}} = \frac{Pl^2}{8}$	$y = \frac{Px^2}{24EI}(l^2 - 2lx + x^2)$ $\Delta = \frac{5Pl^4}{384EI}$	$\Delta_f = \frac{5}{24} \frac{fl^2}{Eh}$	$f = \frac{Pl^2h}{16I}$ $= \frac{Pl^2}{8S_x}$	$P = \frac{16fI}{lh}$ $= \frac{8fS_x}{l}$	$S_x = P(\frac{1}{2} - x)$ $S_a = S_b = \frac{Pl}{2}$ $= R_a = R_b$	1
	$M_x = \frac{P}{4}(2x - \frac{1}{2})(l-x)$ $M_0 = -\frac{Pl^2}{8}$ $M_{\frac{1}{2}} = \frac{9}{16} \frac{Pl^2}{8}$	$y = \frac{Px^3}{576EI}(l-x)(3l-2x)$ $\Delta = \frac{Pl^4}{185EI}$ for $x = 0.578l$	$\Delta_f = \frac{16}{185} \frac{fl^2}{Eh}$	$f = \frac{Pl^2h}{16I}$ $= \frac{Pl^2}{8S_x}$	$P = \frac{16fI}{lh}$ $= \frac{8fS_x}{l}$	$S_x = P(x - \frac{5}{8}l)$ $S_a = \frac{3}{8}Pl = R_a$ $S_b = -\frac{5}{8}Pl = R_b$	1 Distance of pt. of inflection. $x = 0.266l$
	$M_x = \frac{Plx}{2} - \frac{Px^2}{2} - \frac{Pl^2}{12}$ $M_0 = -\frac{Pl^2}{12} = M_l$ $M_{\frac{1}{2}} = \frac{Pl^2}{24}$	$y = \frac{Px^2}{24EI}(l^2 + x^2 - 2lx)$ $\Delta = \frac{Pl^4}{384EI}$ at centre	$\Delta_f = \frac{1}{16} \frac{fl^2}{Eh}$	$f = \frac{Pl^2h}{24I}$ $= \frac{Pl^2}{12S_x}$	$P = \frac{24fI}{lh}$ $= \frac{12fS_x}{l}$	$S_x = P(\frac{1}{2} - x)$ $S_a = S_b = \frac{Pl}{2}$ $= R_a = R_b$	$\frac{3}{2}$ Distance of pt. of inflection $x = 0.2113l$
	$P = \frac{Pl}{6}$ $M_x = \frac{Px^2}{3l^2} - \frac{Px^3}{6l}$ $M_0 = \frac{Pl^2}{5} - \frac{Pl^2}{6}$	$y = \frac{Pl^2}{12EI}(\frac{x}{l} - \frac{x^2}{5l})$ $\Delta = \frac{Pl^3}{15EI}$ at end	$\Delta_f = \frac{2}{5} \frac{fl^2}{Eh}$	$f = \frac{Plh}{6I}$ $= \frac{Pl}{3S_x}$	$P = \frac{6fI}{lh}$ $= \frac{3fS_x}{l}$	$S_x = -\frac{Pl(1-x)^2}{l}$ $= -\frac{Pl(1-x)^2}{2l}$ $S_b = -P$ $S_a = 0$	$\frac{3}{8}$
	$P = \frac{Pl}{3}$ $M_x = \frac{Px}{3}(1 - \frac{x^2}{l^2})$ $= \frac{Px}{6}(l - \frac{x^2}{l})$ $M = \frac{52}{405} Pl$ $= \frac{26}{405} Pl^2$ at $x = 0.5197l$	$\Delta = \frac{47}{3600} \frac{Pl^4}{EI}$ for $x = 0.5197l$	$\Delta_f = \frac{423}{2080} \frac{fl^2}{Eh}$	$f = \frac{26Plh}{405I}$ $= \frac{52Pl}{405S_x}$	$P = \frac{405fI}{26lh}$ $= \frac{405fS_x}{52l}$	$S_x = \frac{1}{3}P - \frac{x^2}{l^2}$ $S_b = -\frac{2}{3}P = R_b$ $S_a = \frac{1}{3}P = R_a$	$\frac{405}{416}$

The Beam and Its Load with the B.M. and S.F. Diagrams.	B.M. Equation and Maximum B.M. M_x or M	Equation of Elastic Line, & Max. Deflection in Terms of The Loading. y or Δ	Max. Deflection in Terms of Stress on Extreme Fiber of Symmetrical Section. Δ_f	Max. Stress on Extreme Fiber in Terms of the Loading Symmetrical Section. f	Breaking Load in Terms of the Fiber Stress. P	S.F. Equation, Max. S.F. & Reactions. S_x, S_a, R_a & R_b	Relative Strength
	$M_x = -Px$ $M_l = -Pl$	$y = \frac{Px^2}{6EI}(3l^2 - 3lx + x^2)$ $\Delta = \frac{Pl^3}{3EI}$ at end	$\Delta_f = \frac{2fl^3}{3Eh}$	$f = \frac{Plh}{2I}$ $= \frac{Pl}{S_x}$	$P = \frac{2fI}{lh}$ $= \frac{fS_x}{l}$	$S_b = -P$ $= R_b$ $S_a = 0$	$\frac{1}{8}$
	$M_x = \frac{Px}{2}$ $M_{\frac{1}{2}} = \frac{Pl}{4}$	$y = \frac{Px^2}{48EI}(3l^2 - 4x^2)$ $\Delta = \frac{Pl^3}{48EI}$ at centre	$\Delta_f = \frac{fl^3}{96Eh}$	$f = \frac{Plh}{8I}$ $= \frac{Pl}{4S_x}$	$P = \frac{8fI}{lh}$ $= \frac{4fS_x}{l}$	$S_a = S_b = \frac{P}{2}$ $= R_a = R_b$	$\frac{1}{2}$
	$x < z_1$ $M_x = \frac{Pz_1x}{l}$ $x > z_1$ $M_x = \frac{Pz_1x}{l} - P(x-z_1)$ $M_{z_1} = \frac{Pz_1z_2}{l}$	$x < z_1$ $y = \frac{Pz_1x^2}{6EI}(2lz_1 - z_1^2 - x^2)$ $x > z_1$ $y = \frac{Pz_1(1-x)}{27EI}(2lx - x^2 - z_1)$ $\Delta = \frac{Pz_1}{27EI} \sqrt{3(z_1(2z_1+z_2))}$ for $x = \frac{1}{3} \sqrt{3(z_1(2z_1+z_2))}$	$\Delta_f = \frac{f}{27Eh} \sqrt{3z_1(2z_1+z_2)}$	$f = \frac{Pz_1z_2h}{2I}$ $= \frac{Pz_1z_2}{S_x l}$	$P = \frac{2fI}{z_1z_2h}$ $= \frac{fS_x}{z_1z_2}$	If $z_1 > z_2$ $S_b = \frac{Pz_1}{l} = R_b$ $S_a = \frac{Pz_2}{l} = R_a$	$\frac{l^2}{8z_1z_2}$
	$x > \frac{l}{2}$ $M_x = \frac{5}{16}P(1-x)$ $x < \frac{l}{2}$ $M_x = \frac{P}{16}(11x-3l)$ $M_{\frac{1}{2}} = \frac{5}{32}Pl$ $M_0 = -\frac{5}{16}Pl$	$x < \frac{l}{2}$ $y = \frac{Px^2}{96EI}(9l-11x)$ $x > \frac{l}{2}$ $y = \frac{P}{96EI}(5l^2 - \frac{5}{2}lx^2 + 12lx^3 - 2x^4)$ $\Delta = \frac{1}{96} \frac{Pl^3}{8EI}$ for $x = l(1 - \frac{1}{\sqrt{5}})$	$\Delta_f = \frac{1}{96} \frac{4fl^3}{15Eh}$	$f = \frac{5Plh}{64I}$ $= \frac{5Pl}{64S_x}$	$P = \frac{64fI}{5hl}$ $= \frac{64fS_x}{5l}$	$S_b = -\frac{11}{16}P = R_b$ $S_a = \frac{5}{16}P = R_a$	$\frac{8}{5}$ Distance of Pt. of inflection $x = \frac{3}{11}l$
	$R_a = \frac{P}{2l}(3lz_2^2 - z_2^3)$ $x < z_2$ $M_x = R_a(1-x) - R_z(x-z_2)$ $x > z_2$ $M_x = R_a(1-x)$ $M_{z_2} = R_a(1-z_2)$ $M_0 = R_a l - Pz_2$	$x < z_2$ $y = \frac{P}{6EI}(R_a^2 - 3R_a x^2 + 3Pz_2^2 x^2 - P x^3)$ $x > z_2$ $y = \frac{P}{6EI}(R_a^2 - 3R_a x^2 + 3Pz_2^2 x - Pz_2^2)$ $\Delta = \frac{Pz_2}{6EI}(1-z_2) \sqrt{\frac{1-z_2}{3l-z_2}}$ for $x = l(1 - \sqrt{\frac{1-z_2}{3l-z_2}})$	$\Delta_f = \frac{2f}{3Eh} \sqrt{(3l-z_2)(1-z_2)}$	$f = \frac{Ph}{4I}(3lz_2^2 - z_2^3)(1-z_2)$ $= \frac{P}{2I} (3lz_2^2 - z_2^3)(1-z_2)$	$P = \frac{4fI}{z_2^2(3l-z_2)(1-z_2)h}$ $= \frac{2fI S_x}{z_2^2(3l-z_2)(1-z_2)}$	$S_a = \frac{P}{2l}(3lz_2^2 - z_2^3) = R_a$ $S_b = R_a - P = R_b$	$\frac{l^3}{4z_2^2(3l-z_2)(1-z_2)}$ when $z_2 > 586l$ $M_{z_2} > M_0$ $M_{z_2} = 17Pl$

The Beam and its Load with the B.M. and S.F. Diagrams	B.M. Equation and Maximum B.M. M_x & M_c	Equation of Elastic Line, & Max. Deflection in Terms of The Loading. y & Δ	Max. Deflection in Terms of Stress on Extreme Fiber of Symmetrical Section. Δf	Max. Stress on Extreme Fiber in Terms of the Loading Symmetrical Section. f	Breaking weight in Terms of the Fibre stress P	S.F. Equation, Max. S.F. and Reactions. S_x, S_c, R_a & R_b	Relative Strength
	$M_x = \frac{Pl^2}{60} (10 \frac{x^3}{l^3} - 9 \frac{x^2}{l^2} + 2)$ $M_a = -\frac{1}{15} Pl$ $M_c = -\frac{1}{10} Pl$ $M = \frac{2Pl^2}{15} \cdot \frac{1}{9} Pl = 0.429 Pl$ at $x = 11\sqrt{\frac{10}{18}} = 0.548 l$	$y = \frac{Pl^3}{60EI} (2 \frac{x^4}{l^4} - 3 \frac{x^3}{l^3})$ $\Delta = \frac{Pl^3}{384EI}$ for $x = 0.525 l$	$\Delta f = \frac{10 fl^2}{192 Eh}$	$f = \frac{Plh}{20 I}$ $= \frac{Pl}{10 S_m}$	$P = \frac{20 fl}{lh}$ $= \frac{10 f S_m}{l}$	$S_x = \frac{1}{3} P - \frac{x^2}{l^2} P$ $S_b = -\frac{2}{3} P = R_b$ $S_a = \frac{1}{3} P = R_a$	$\frac{5}{4}$
	for $x < \frac{l}{2}$ $M_x = Px (\frac{1}{2} - \frac{2}{3} \frac{x^2}{l^2})$ $M_c = \frac{Pl}{6}$	$y = \frac{Pl^3}{12EI} (\frac{5}{8} \frac{x^4}{l^4} - \frac{x^3}{l^3})$ $\Delta = \frac{Pl^3}{60EI}$ at centre	$\Delta f = \frac{1}{5} \frac{fl^2}{Eh}$	$f = \frac{Plh}{12 I}$ $= \frac{Pl}{6 S_m}$	$P = \frac{12 fl}{lh}$ $= \frac{6 f S_m}{l}$	for $x < \frac{l}{2}$ $S_x = P (\frac{1}{2} - \frac{2x^2}{l^2})$ for $x > \frac{l}{2}$ $S_x = -P (\frac{1}{2} - \frac{2(1-x)^2}{l^2})$ $S_a = \frac{1}{2} P = R_a$ $S_b = -\frac{1}{2} P = R_b$	$\frac{3}{4}$
	for $x < \frac{l}{2}$ $M_x = -\frac{Pl}{48} (\frac{5x^3}{l^3} - \frac{x}{l})$ $M_a = M_b = -\frac{3}{48} Pl$ $M_c = \frac{Pl}{16}$	$y = \frac{Pl^3}{6EI} (\frac{5x^4}{16l^4} - \frac{x^3}{2l^3})$ $\Delta = \frac{7Pl^3}{1920EI}$ at centre	$\Delta f = \frac{7}{100} \frac{fl^2}{Eh}$	$f = \frac{5Plh}{96 I}$ $= \frac{5Pl}{48 S_m}$	$P = \frac{96 fl}{51 lh}$ $= \frac{48 f S_m}{5 l}$	for $x < \frac{l}{2}$ $S_x = P (\frac{1}{2} - \frac{2x^2}{l^2})$ $S_a = \frac{1}{2} P = R_a$ $S_b = -\frac{1}{2} P = R_b$	$\frac{6}{5}$
	for $x < \frac{l}{2}$ $M_x = Px (\frac{1}{2} - \frac{x}{l} - \frac{2x^3}{3l^3})$ $M_c = \frac{Pl}{12}$	$y = \frac{Pl^3}{12EI} (\frac{3}{8} \frac{x^4}{l^4} - \frac{x^3}{l^3} + \frac{x^2}{l^2} - \frac{2}{3} \frac{x^5}{l^5})$ $\Delta = \frac{3}{320} \frac{Pl^3}{EI}$	$\Delta f = \frac{9}{40} \frac{fl^2}{Eh}$	$f = \frac{Plh}{24 I}$ $= \frac{Pl}{12 S_m}$	$P = \frac{24 fl}{lh}$ $= \frac{12 f S_m}{l}$	for $x < \frac{l}{2}$ $S_x = \frac{2(\frac{1}{2} - x)^2}{l^2} P$ for $x > \frac{l}{2}$ $S_x = \frac{2(x - \frac{1}{2})^2}{l^2} P$ $S_a = -\frac{1}{2} P = R_a$ $S_b = -\frac{1}{2} P = R_b$	$\frac{3}{2}$
	$M_x = \frac{x(1-x)}{6l} \{ R(2l-x) + P_x(l+x) \}$ $M_c = \frac{l^2}{6} \frac{r-p}{(R-P)} \{ (2P_r + P_x) (R-P) - (r^2 + p^2 - 2Pr) \}$ at $x = \frac{l}{3} \frac{r-p}{R-P}$ where $r = \sqrt{\frac{P^2 + R^2 + PR}{3}}$					$S_x = R_a - \frac{M + P_x x}{l}$ $S_a = \frac{l}{6} (2P_r + P_x) = R_a$ $S_b = -\frac{l}{6} (2P_p + P_x)$ where $\frac{R^2 + P^2 + PR}{3} = \frac{R^2 + P^2 + PR}{3}$	

The Beam and its Load with the B.M. and S.F. Diagrams.	B.M. Equation and Maximum B.M. M_x & M	Equation of Elastic Line, & Max. Deflection in Terms of The Loading. y & Δ	Max. Deflection in Terms of Stress on Extreme Fiber of Symmetrical Section. Δ_f	Max. Stress on Extreme Fiber in Terms of the Loading Symmetrical Section. f	Breaking Weight in Terms of the Fiber Stress P	S.F. Equation, Max. S.F. and Reactions S_x, S, R_a, R_b	Relative Strength
	$x < \frac{l}{2}$ $M_x = \frac{P}{4}(2x - \frac{l}{2})$ $x > \frac{l}{2}$ $M_x = \frac{P}{4}(\frac{3}{2}l - 2x)$ $M_o = M_l = -\frac{Pl}{8}$	$x < \frac{l}{2}$ $y = \frac{Px^2}{84EI}(3l - 2x)$ $x > \frac{l}{2}$ $y = \frac{P}{24EI}(2x^2 + 15l^2x - \frac{3}{2}l^2 - \frac{3}{2}lx^2)$ $\Delta = \frac{Pl^3}{192EI}$	$\Delta_f = \frac{fl^2}{12Eh}$	$f = \frac{Phl}{16I}$ $= \frac{Pl}{8S_m}$	$P = \frac{16fl}{hl}$ $= \frac{8fS_m}{l}$	$S_a = S_b = \frac{P}{2}$ $= R_a = R_b$	1 Distance of Pt. of inflection. $x = \frac{l}{4}$
	$R_a = Pz_1/(z_1+z_2)$ $M_o = -Pz_1z_2/l$ $x < z_1$ $M_x = R_ax + M_o$ $x > z_1$ $M_x = R_ax - P(x-z_1) + M_o$	$x < z_1$ $y = \frac{Px^2z_1}{6EIP}(3z_1 - (z_1+z_2)x)$ $x > z_1$ $y = \frac{Px^2z_1}{6EIP}(3z_1 - 3x^2 - 3z_1x) - \frac{P}{6EIP}(x-z_1)^2(3z_1+z_2)x$ $\Delta = \frac{Pz_1^2z_2^2}{3EI(z_1+z_2)^2}$ for $x = \frac{z_1z_2}{z_1+z_2}$	$\Delta_f = \frac{9fz_1^2z_2^2}{E(z_1+z_2)^2hl}$	$f = \frac{Pz_1z_2h}{2IU}$ $= \frac{Pz_1z_2}{l^2S_m}$	$P = \frac{2fIU}{z_1z_2h}$ $= \frac{fI^2S_m}{z_1z_2^2}$	$S_a = Pz_1/(z_1+z_2) = R_a$ $S_b = -Pz_2/(z_1+z_2) = R_b$	$\frac{l^3}{8z_1z_2^2}$ Distance of pt. of inf. $x_o = \frac{z_1}{z_1+z_2}l$ $x_l = \frac{z_2^2+z_1l}{z_1+z_2}$
	$x < z$ $M_x = Px$ $x > z$ $M = Pz$	$x < z$ $y = \frac{Px^3}{6EI}(3l - 3z^2 - x^2)$ $x > z$ $y = \frac{Pz^3}{6EI}(3lx - 3x^2 - z^2)$ $\Delta = \frac{Pz^3}{6EI}(\frac{3}{4}l^2 - z^2)$ at centre	$\Delta_f = \frac{f}{3Eh}(\frac{3}{4}l^2 - z^2)$	$f = \frac{Phz}{2I}$ $= \frac{Pz}{S_m}$	$P = \frac{2fI}{hz}$ $= \frac{fS_m}{z}$	$S_a = S_b = P$ $= R_a = R_b$ at middle portion $S = 0$	$\frac{l}{8z}$
	$x < z$ $M_x = Px + \frac{Pz^2}{l} - Pz$ $x > z$ $M = \frac{Pz^2}{l}$ $M_o = M_l = -Pz(-\frac{z}{l})$	$x < z$ $y = \frac{Px^2}{6EI}(3lz - 3z^2 - xl)$ $x > z$ $y = \frac{Pz^2}{6EI}(3lx - 3x^2 - z)$ $\Delta = \frac{Pz^2}{12EI}(\frac{3}{2}l - 2z)$ at centre	$\Delta_f = \frac{fl}{6Eh}(\frac{3}{2}l - 2z)$	$f = \frac{Phz^2}{2Il}$ $= \frac{Pz^2}{S_m l}$	$P = \frac{2fIl}{hz^2}$ $= \frac{fI^2S_m}{z^2}$	$S_a = S_b = P$ in middle portion $S = 0$	$\frac{l^3}{8z^2}$ Distance of point of inflection $x = z - \frac{z^2}{2l}$
	$M_x = -\frac{Px^2}{2}$ $M_o = -\frac{Pl^2}{2}$	$y = \frac{Px^3}{24EI}(x^2 - 4l^2x + 3l^3)$ $\Delta = \frac{Pl^4}{8EI}$	$\Delta_f = \frac{fl^2}{2Eh}$	$f = \frac{Pl^2h}{4I}$ $= \frac{Pl}{2S_m}$	$P = \frac{4fl}{lh}$ $= \frac{2fS_m}{l}$	$S_x = -P(l-x)$ $S_b = -Pl$ $S_a = 0$	$\frac{1}{4}$



$$M = Nc_b d^2 \quad \text{in thousands.}$$

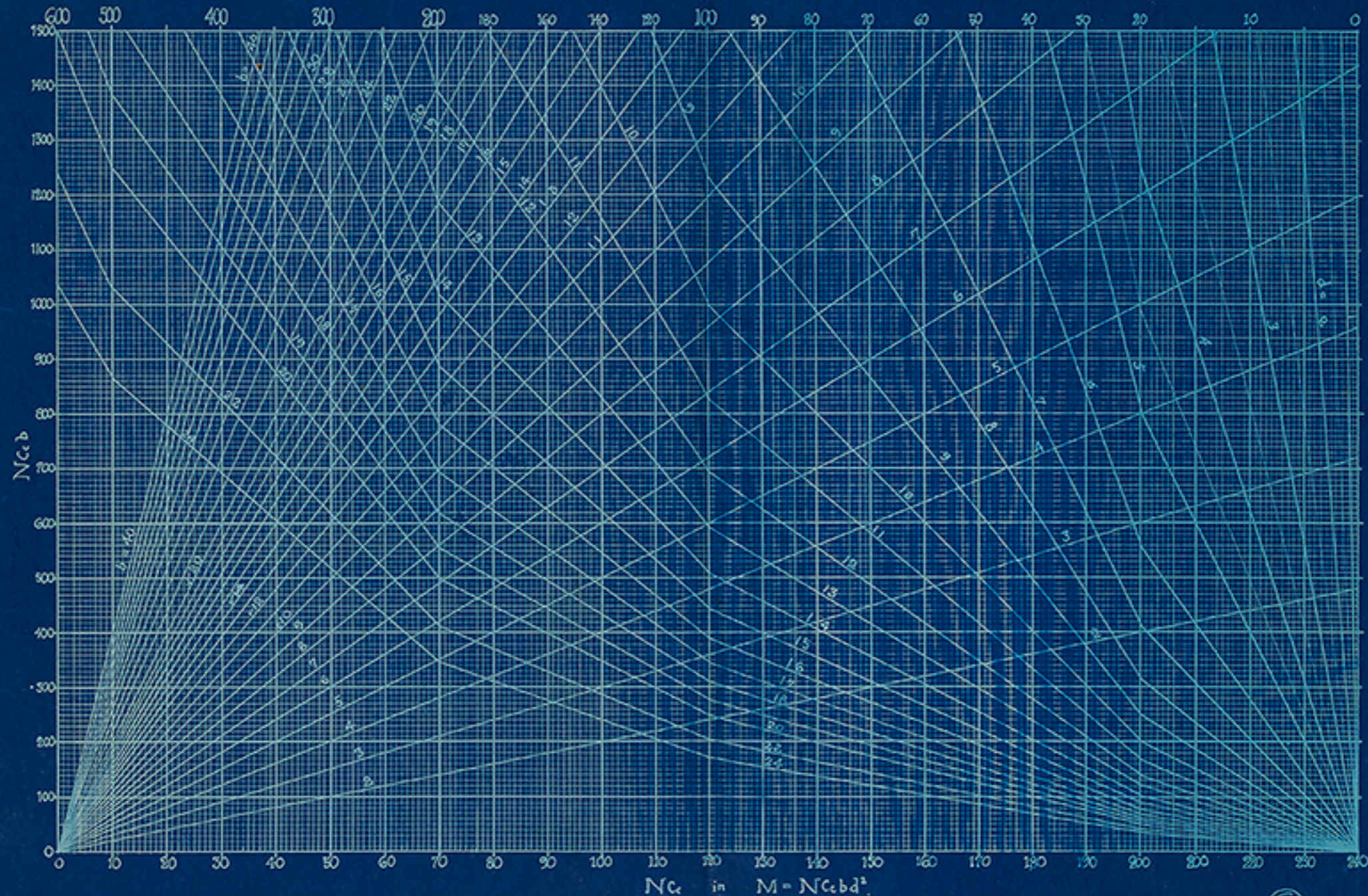


DIAGRAM FOR RESISTING MOMENT OF BEAMS.



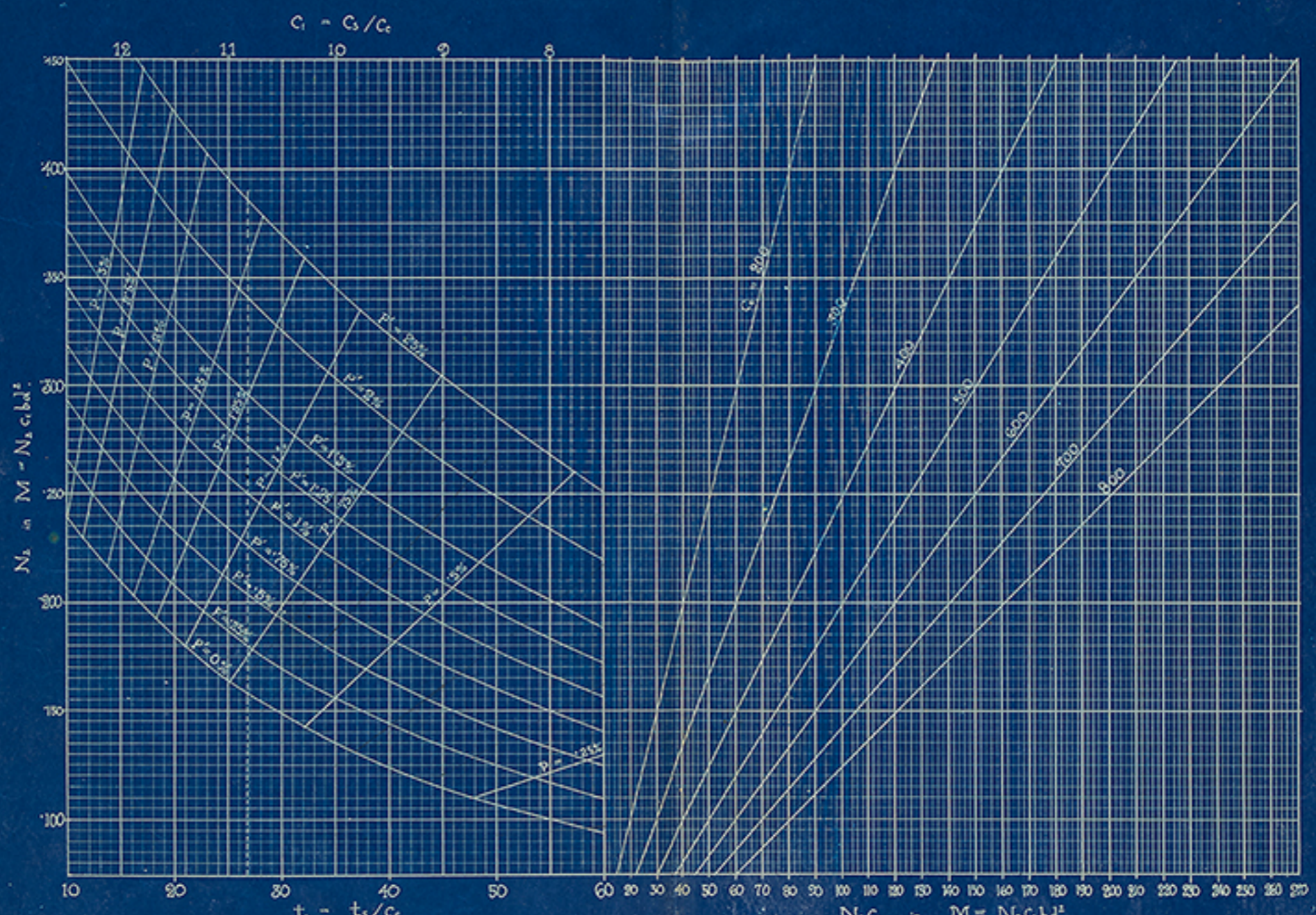
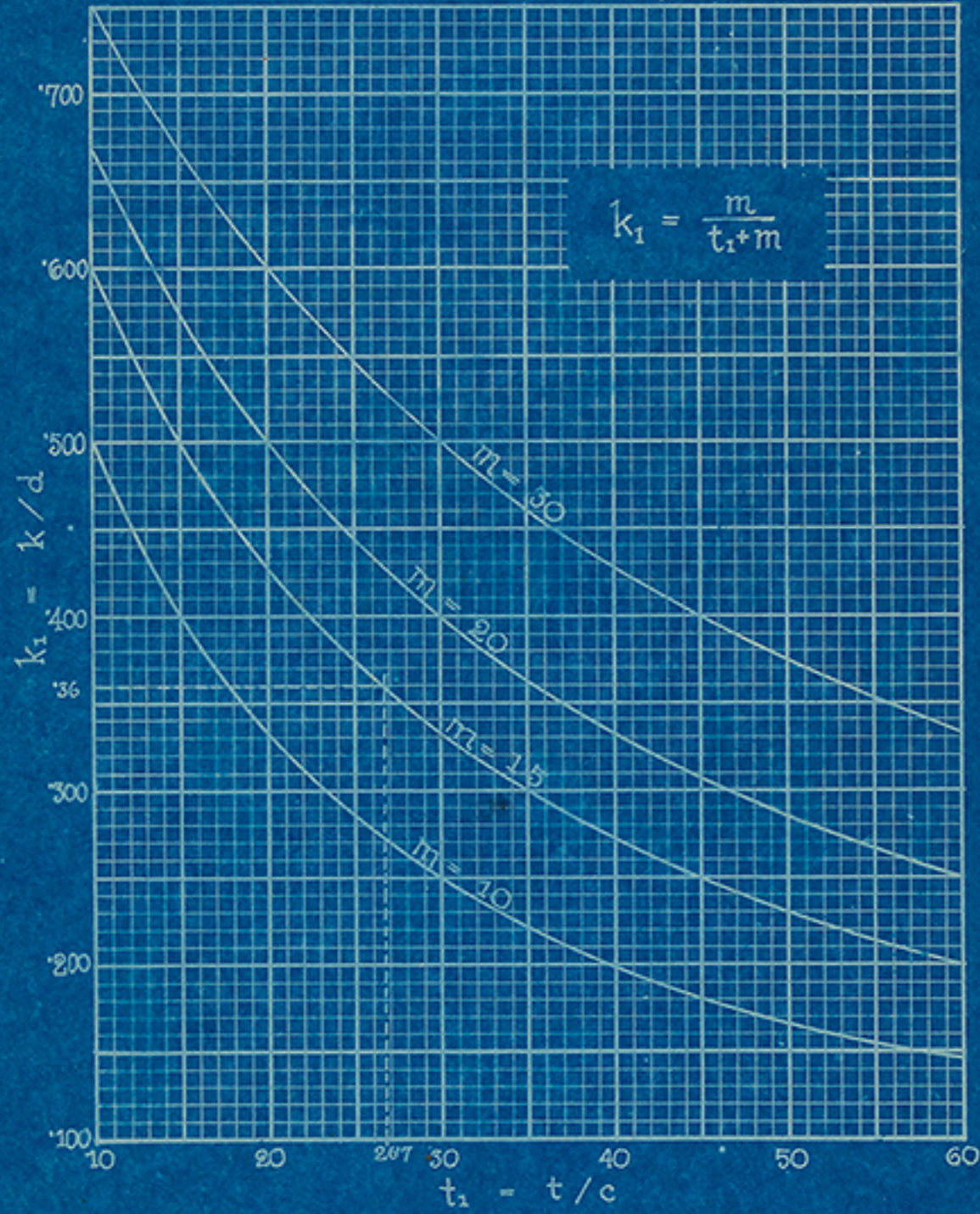
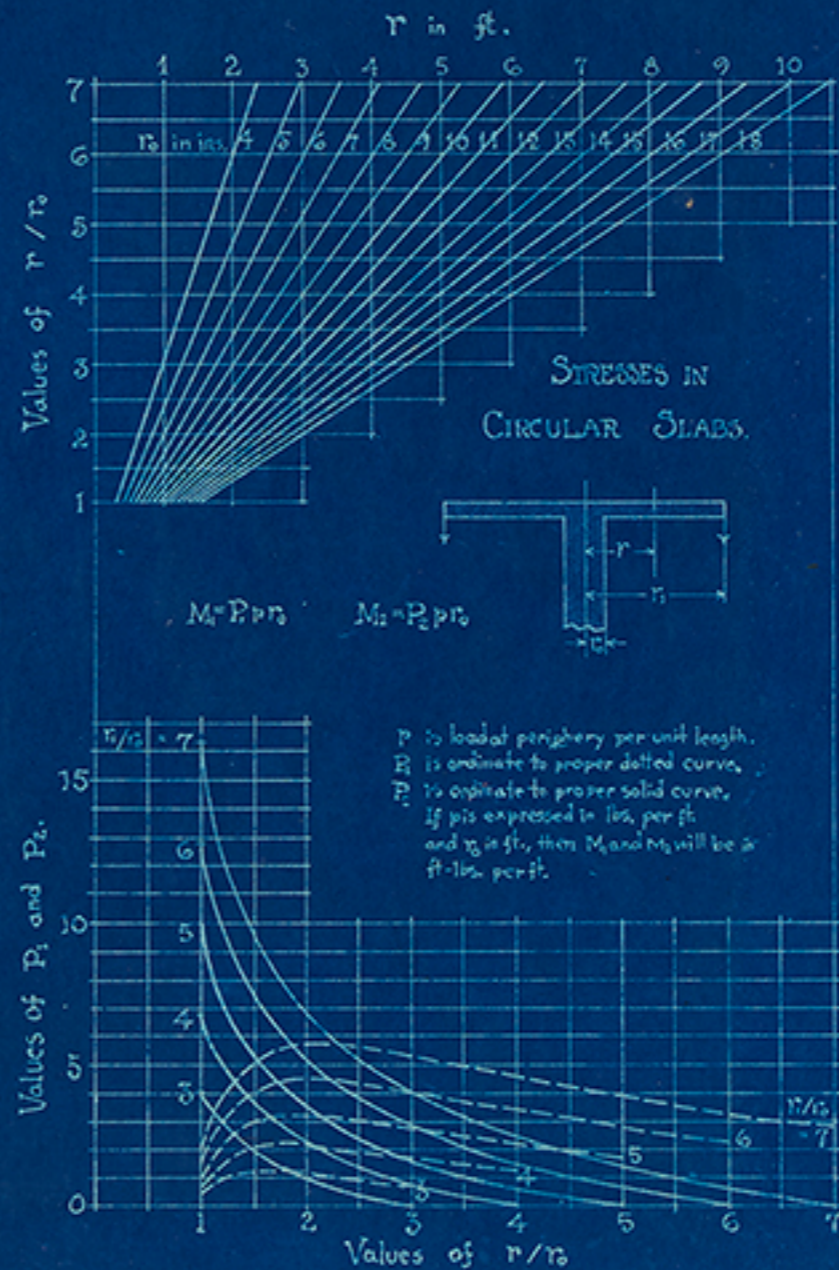
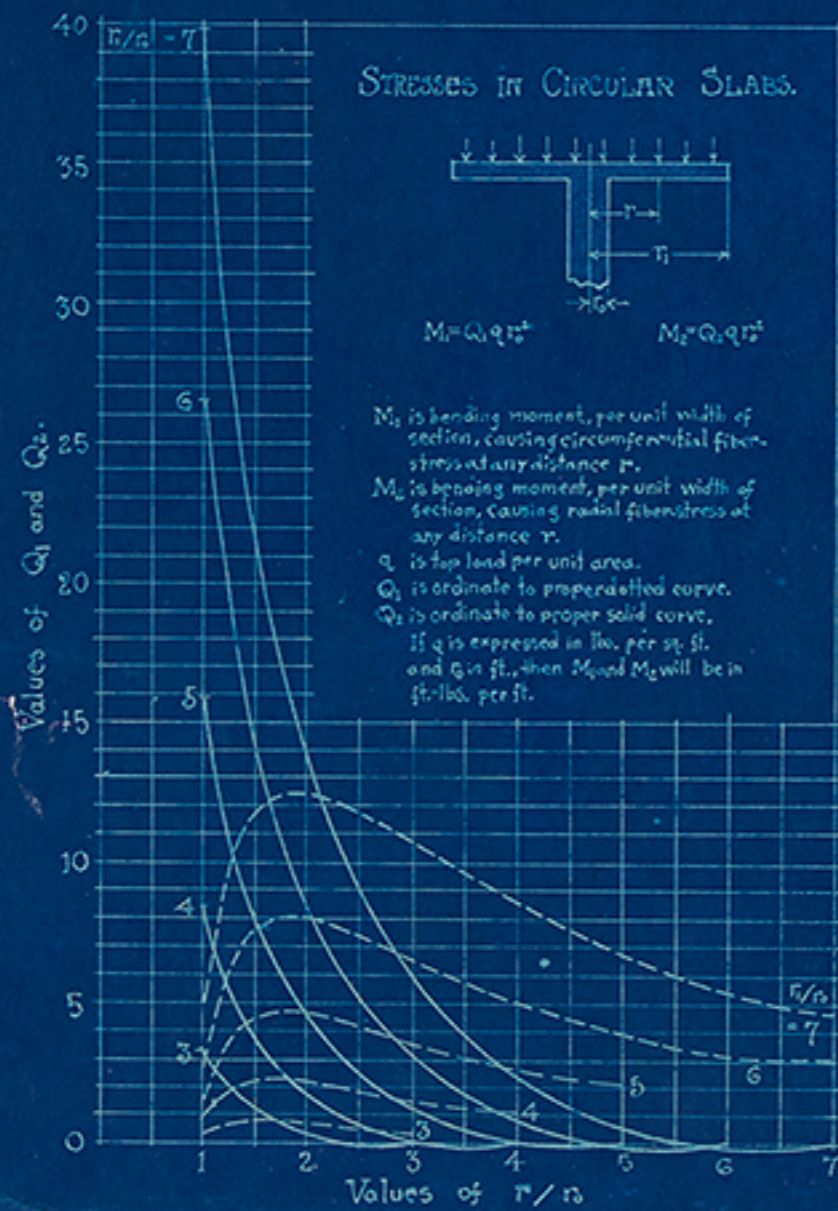


DIAGRAM FOR DOUBLE REINFORCED RECTANGULAR BEAM. $\frac{d_s}{d} = \frac{1}{10}$. 

DEPTH OF NEUTRAL AXIS
FOR VARIOUS RATIO OF STRESSES.



(Based upon the analysis presented by Prof. H. T. Eddy for homogeneous plates. The value of Poisson's ratio assumed in the numerical substitutions has been 0.1.)



C_c	Total <u>compression</u> on <u>concrete</u> .
C_s	Total <u>compression</u> on <u>steel</u> .
c	<u>Compressive</u> stress intensity.
c	<u>Compressive</u> stress intensity on concrete.
C_p	Compressive stress in column not hooped.
C'	Minimum <u>compressive</u> stress in concrete for combined bending and direct load.
C_s	<u>Compressive</u> stress intensity on steel.
C_r	Ratio C_s/c .
C'_s	Minimum <u>compressive</u> stress in <u>steel</u> for combined bending and direct load.
C^2	<u>Compressive</u> stress intensity in long column.
d	<u>Depth</u> .
d	Effective <u>depth</u> of a beam from top of a beam to axis of tensile reinforcement.
d_s	Total <u>depth</u> of a <u>slab</u> in a T-beam.
d_c	<u>Depth</u> or distance of the centre of <u>compressive</u> reinforcement from the compressed edge.
d'	Distance of the centre of reinforcement from any edge.
d	Any <u>diameter</u> .
d	<u>Outside diameter</u> .
d_i	<u>Inside diameter</u> .

LIST OF SYMBOLS

A	<u>Area</u> .
A	Total cross-sectional <u>area</u> of a pillar.
A_1	<u>Area</u> of concrete.
A_L	Cross-sectional <u>area</u> of <u>longitudinal</u> steel rods in a pillar.
A_H	Cross-sectional <u>area</u> of a <u>hooped</u> reinforcing rod in a pillar.
A_e	<u>Equivalent area</u> .
A_c	<u>Area</u> of <u>compressive</u> reinforcement in beams.
A_T	<u>Area</u> of <u>tensile</u> reinforcement in beams.
A_s	<u>Area</u> of <u>shear</u> reinforcement.
A_t	<u>Total area</u> .
a	Buckling factor of a column.
B_b	Ratio I/l for <u>beams</u> , i.e. a measure of stiffness.
B_c	Ratio I/l for column.
b	<u>Breadth</u> .
b	<u>Breadth</u> of rectangular beam.
b_r	<u>Breadth</u> of the <u>rib</u> in a T-beam.
b_s	Effective <u>breadth</u> of the <u>slab</u> in a T-beam.
C	Total <u>compressive</u> force or stress.

d_c	Diameter of the core of a pillar with hooped reinforcement.
d_l	Diameter of a longitudinal reinforcing rod of a pillar.
d_h	Diameter of a helical reinforcing rod of a pillar.
d_b	Diameter of stirrup bar.
E	Elastic modulus of any materials.
E_c	Elastic modulus of concrete in compression.
E_s	Elastic modulus of steel.
e	Eccentricity of any load.
e_c	Unit elongation of concrete.
e_s	Unit elongation of steel.
F	Total friction between any two surfaces.
f	Friction or adhesion between surfaces in unit of force per unit of area.
f	Intensity of stress (general)
f	Fiber stress intensity.
f_c	Compressive stress intensity.
f_t	Tensile stress intensity.
f_b	Bearing stress intensity.
f_u	Intensity of ultimate stress.
g	Gravity.

H	Horizontal component of force.
h	Intensity of horizontal shearing stress.
h	Any height.
h	Total height of beam.
I	Inertia moment.
I_x	Inertia moment on axis XX.
I_y	Inertia moment on axis YY.
I_s	Inertia moment for steel.
I_c	Inertia moment for concrete.
I_e	Inertia moment for equivalent section.
I_n	Inertia moment on neutral axis.
I_g	Inertia moment on gravity axis.
i	Radius of gyration.
j	Arm of any couple, i.e. distance between two parallel force of equal magnitude, but acting in opposite directions.
j	Arm of the couple formed by the compressive and tensile forces in beam.
j_s	Ratio j/d .
K	A constant.

k	Distance of the neutral axis from the compressed edge of a beam.
k_d	Ratio k/d .
k'	In beams with combined bending and direct stress, distance of neutral axis from more compressed edge of the beam.
l	<u>Length</u>
l	<u>Effective length</u> or span of a beam or arch.
l_1	<u>Longer</u> span of a rectangular slab.
l_2	<u>Shorter</u> span of a rectangular slab.
M	<u>Bending moment</u> .
M	Any <u>moment</u> .
M_{max}	<u>Maximum bending moment</u> of the external forces or loads on a beam.
M_x	<u>Bending moment</u> at a distance x from left abutment.
M_f	<u>Fixing moment</u> of built in beam.
M_c	<u>Bending moment</u> at centre of beam.
M_e	<u>Bending moment</u> at end of beam.
M_s	<u>Statical moment</u> or first moment of area.
M_l	<u>Bending moment</u> of longer beam.
M_s	<u>Bending moment</u> of shorter beam.
M	<u>Maximum bending moment</u> on beam supported at both ends and not continuous.
m	<u>Modular ratio</u> , E_s/E_c .

N_1	Constants in stress formulas.
N_2	
N_3	
N_4	
n	Any <u>number</u>
n	<u>Number</u> of reinforcing bars.
n_s	<u>Number</u> of bars to be bent.
O	Perimeter of any regular or irregular figure.
P	Total <u>pressure</u> on a given area.
p	Intensity of <u>pressure</u> per unit of length or area in any direction.
p	<u>Percentage</u> of steel, i.e. $p = 100r$
R	<u>Reaction</u> of a beam on its support.
R	<u>Resistance moment</u> of the internal stresses in a beam at a given cross-section.
R_L	<u>Left reaction</u> .
R_R	<u>Right reaction</u> .
r	<u>Radius</u> .
r_i	<u>Inner radius</u> .
r	<u>Ratio</u> .

r	Ratio of area of steel to area of concrete in singly reinforced beams.
r_t	Ratio of area of steel in <u>tension</u> to area of concrete in doubly reinforced beams.
r_c	Ratio of area of steel in <u>compression</u> to area of concrete.
S	Total <u>shearing</u> force.
s	<u>Shearing</u> stress intensity.
s	Shearing stress intensity on concrete.
S_r	Safety factor.
T	Total <u>tensile</u> force.
T	Total <u>tensile</u> stress on a given cross-section.
T_c	Total <u>tension</u> on <u>concrete</u> , when necessary to discriminate.
T	Total <u>tension</u> on steel.
T_d	Total <u>diagonal tension</u> .
t	<u>Tensile</u> stress intensity.
t	<u>Tensile</u> stress intensity on steel.
t_c	<u>Tensile</u> stress intensity on <u>concrete</u> .
t_r	Ratio of stress, t/c
t_d	Intensity of <u>diagonal tension</u> .
u	<u>Ultimate</u> stress in a material.
u	The distance of the centre of compression from compressed edge of a beam.

V	<u>Volume</u> .
V	<u>Volume</u> of hooped core of column.
V_h	<u>Volume</u> of <u>hooped</u> reinforcement in a column.
V_l	<u>Volume</u> of <u>longitudinal</u> reinforcement in a column.
V	<u>Vertical</u> component of force.
v	Intensity of vertical component of force.
W	<u>Weight</u> or load.
W_f	<u>Working</u> factor, i.e. $1/S_r$
w	<u>Weight</u> per unit of length.
w	<u>Weight</u> per unit of area.
w	<u>Weight</u> per unit of volume.
x	Any unknown quantity.
x	Independent variable in any function.
x	Horizontal coordinate of a point.
x_1	Distance from the support to the point where no shear reinforcement are required.
x_2	Distance from the support to the point where the horizontal reinforcement may be bent.
y	A second unknown quantity.
y	Dependent variable corresponding with x .

- y Vertical co-ordinate of a point.
 Z Section modulus.
 z A third unknown quantity.
 z Distance between any two stirrups.
 α Denominator in formula $M = \frac{pl^2}{\alpha}$.
 Δ Deflection.
 θ Any angle.
 ξ Ratio of depth d_s/d in T-beam.
 ν Ratio of depth d_c/d in doubly reinforced beam.
 γ Ratio of breadth to depth in rectangular beam.



- A Area
- A Total area.
- A Total cross-sectional area of a pillar.
- A_e Equivalent area (等値面積)
- A_o Cross-sectional area of a hooped reinforcing rod in a pillar (柱、有効断面積)
- a Area of reinforcement. (鉄筋断面積)
- a Total area of reinforcement in beams. $a_t + a_c$
- a_c Area of compressive reinforcement in beams. (圧縮鉄筋断面積)
- a_t Area of tensile reinforcement in beams (応張鉄筋断面積)
- a_r Area of reinforcement in minor compression side in case of combined stress.
- a_s Area of shear reinforcement. (応剪鉄筋断面積)

B 柱ノ太サ (曲ル方向ニ直サ) ^{ニトク} 寸法

B Effective breadth of ^{the} slab in a T-beam.

b Breadth of a rectangular beam.

b Breadth of ^{the} rib in a T-beam.

C

C₁ } Constants in stress formula.

C₂ }

⋮

D. Diameter of the core of a pillar with hooped reinforcement
巻筋ニハ巻筋 中心内ノ直径

D 柱ノ直径 又ハ柱ノ曲ル方向 ^{ニトク} 断面ノ寸法

D Total depth of a beam.

* D Outside diameter.

d Effective depth of a beam or distance of the center
of tensile reinforcements from the top of
a beam. from top of beam to axis of
tensile reinforcement.

* d Diameter.

E Elastic modulus.

cE Elastic modulus of concrete.

sE Elastic modulus of steel.

e Eccentricity of any load.

ϵ Modular ratio, $\frac{E_s}{E_c}$.

F Force (力)

f Stress intensity (応力度)

f_a Bond stress intensity (応力係数)

f_b Bending stress

Member		Stress \mathcal{R}		Length ft.	Least Reqd. of dynation in ²	Unit Loading lb per in ²	Area Required A' in ²	Make up Members			Area Used A' in ²	Weight per ft	\mathcal{R} for total Length	22 in. Number of Rivet
								Shape	Section	no.				
F-8	+	5,200	5,400	3'5"	488	9,950	.548	2L3	2x2x'175	2-'670	4-2'28	16	2	
I-11	+	5,400	"	"	"	"	"	"	"	"	"	"	4	
8-9	-	2,300	3,900	3'8 1/2	/	16,500	.252	1L	2 1/2 x 2 x '175	.750	2'57	10	"	
10-11	-	3,900	"	"	/	"	"	"	"	"	"	"	"	
2-3	-	3,000	3,000	4'3 6/15	/	"	.194	1L	2x2x'175	.670	2'28	"	"	
16-17	-	2,100	"	"	/	"	"	"	"	"	"	"	"	
5-6	-	5,400	5,400	"	/	"	.349	2L3	"	2-'670	2-2'28	20	"	
13-14	-	4,400	"	"	/	"	"	"	"	"	"	"	"	
5-N	-	14,800	22,000	6'	/	"	1'47	"	3x2x'250	2-1'181	2-4'04	49	5	
14-N	-	10,200	"	"	/	"	"	"	"	"	"	"	"	
7-N	-	22,000	"	"	/	"	"	"	"	"	"	"	3	
12-N	-	16,700	"	"	/	"	"	"	"	"	"	"	"	
O-1	-	36,700	36,700	"	/	"	.237	"	3x2 1/2 x '250	2-1'312	2-4'46	54	8	
0-18	-	30,300	"	"	/	"	"	"	"	"	"	"	"	
O-3	-	32,500	"	"	/	"	"	"	"	"	"	"	7	
0-16	-	27,700	"	"	/	"	"	"	"	"	"	"	"	
O-N	-	18,100	18,100	12'	/	"	1'17	"	2 1/2 x 2 x '175	2-'757	2-2'57	62	4	

$$\left. \begin{aligned} t_1 &= 30 \\ \text{従} \text{て } k_1 &= \frac{1}{3} \\ \text{従} \text{て } r &= 0.056 \end{aligned} \right\}$$

$$\begin{aligned} d &= \sqrt{\frac{6t_1(t_1+m)^2}{m(3t_1+2m) \cdot t} \cdot \frac{M}{b}} = \sqrt{\frac{6 \times 30(45)^2}{15(90+30) \cdot 15,000} \cdot \frac{M}{b}} \\ &= \sqrt{\frac{6 \times 30 \times 2025}{15 \times 150,000} \cdot \frac{M}{b}} = \sqrt{\frac{2025}{150,000} \cdot \frac{M}{b}} = \sqrt{0.0135 \cdot \frac{M}{b}} \\ &= \frac{3674}{1162} \sqrt{\frac{M}{b}} = 0.1162 \sqrt{\frac{M}{b}} \end{aligned}$$

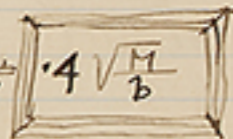
$$\begin{aligned} d &= \sqrt{\frac{6(t_1+m)^2}{m(3t_1+2m) \cdot C} \cdot \frac{M}{b}} = \sqrt{\frac{6 \times 2025}{15 \times 150,000 \times 3} \cdot \frac{M}{b}} \\ &= \sqrt{\frac{27}{2,100} \cdot \frac{M}{b}} = \sqrt{0.135 \cdot \frac{M}{b}} \end{aligned}$$

$$= \sqrt{\frac{1}{741} \cdot \frac{M}{b}} = \frac{1}{86} \sqrt{\frac{M}{b}}$$

$$\text{c. } M \sim 1/15 \text{ } M = M' \times 12$$

$$d = \sqrt{162} \sqrt{\frac{M}{b}} = 12.727 \sqrt{\frac{M}{b}} \Rightarrow 4 \sqrt{\frac{M}{b}}$$

$$\text{2. } \sqrt{\frac{1}{618}} \sqrt{\frac{M}{b}} = \frac{1}{24.85} \sqrt{\frac{M}{b}}$$



$$d = .4 \sqrt{\frac{M}{b}} \quad M = \frac{Wl}{8}$$

$$W = 48000 \quad \frac{W}{8} = 6,000 \quad \frac{.4}{1.73} = .231$$

l	W/8	b = 3 * V3 = 173		
		M	VM	VM * 4
2	12,000	10,000	100	231
3	18,000	23,000	141	
4	24,000	31,000	173	
5	30,000	40,000	200	
6	36,000	50,000	224	
7	42,000	60,000	245	
8	48,000	70,000	265	
9	54,000	80,000	283	
10	60,000	90,000	300	
12	72,000	100,000	316	
14	84,000	120,000	346	
16	96,000	140,000	374	
18	108,000	160,000	400	
20	120,000	180,000	424	
22	132,000	192,000		
24	144,000	204,000		
26	156,000	216,000		
28	168,000			
30	180,000			

l	M	VM	b = 3 * V3 = 173				b = 6		b = 8		b = 9
			VM/173	VM/173	VM/173	VM/173	VM/173	VM/173	VM/173	VM/173	
2	10,000	316	73	62	56	516	477	449	422		
3	2,000	447	103	89	79	713	675	63	595		
4	3,000	548	127	109	98	819	826	775	713		
5	4,000	632	146	126	113	1013	953	895	814		
6	5,000	707				1216	115	109	10	914	
7	6,000	775				138	129	119	11	104	
8	7,000	837				149	139	126	118	112	
9	8,000	894					146	135	127	119	
10	9,000	949					155	143	134	123	
12	10,000	100					163	151	141	126	
14	20,000	141					326	302	282		
16	30,000	173									
18	40,	200									
20	50,	224									
22	60,	245									
24	70,	265									
26	80,	283									
28	90,	300									
30	100,	316									
	120,	346									

(Based upon the analysis presented by Prof. H. T. Eddy for homogeneous plates. The value of Poisson's ratio assumed in the numerical substitutions has been 0.1.)

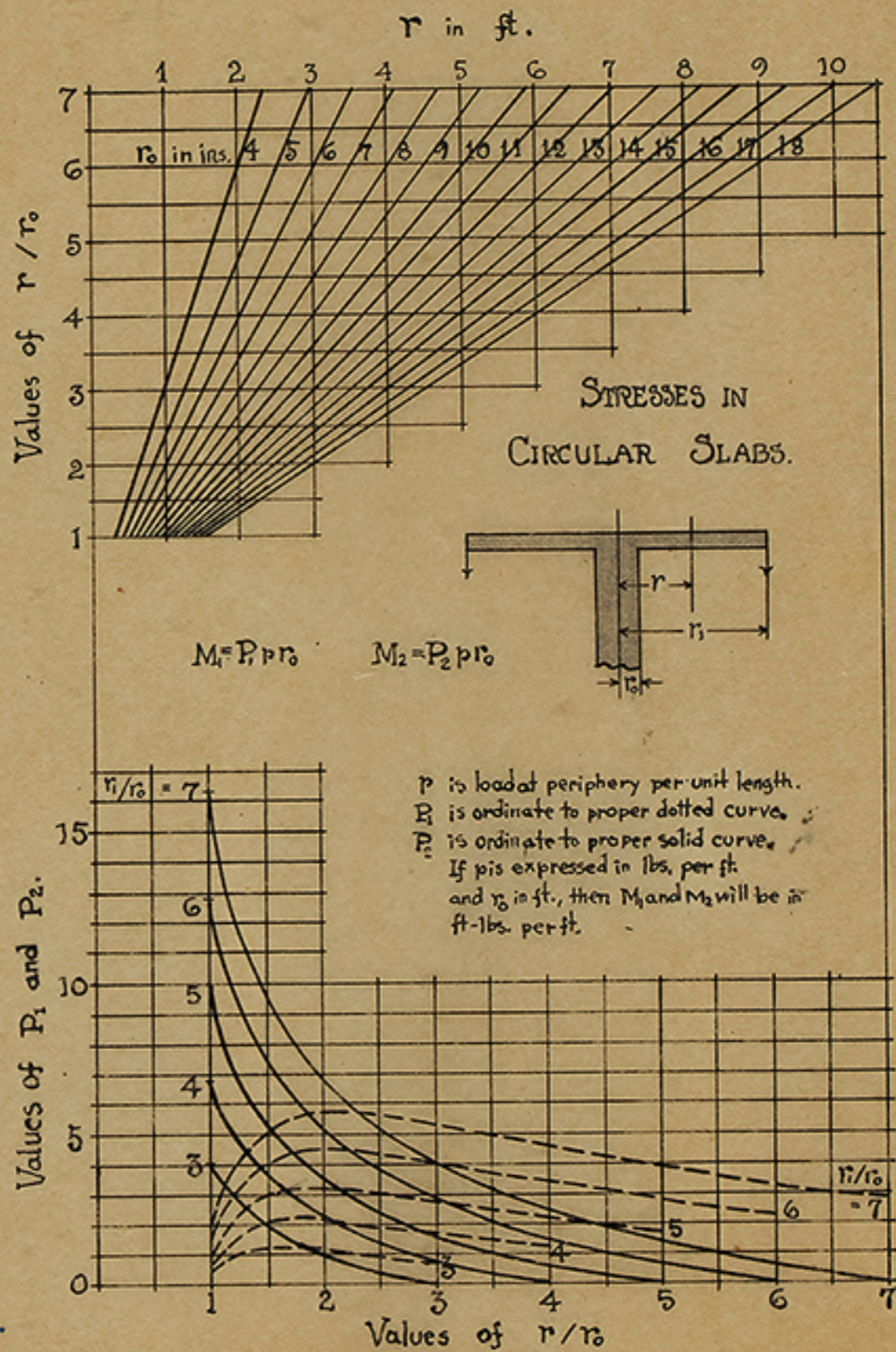
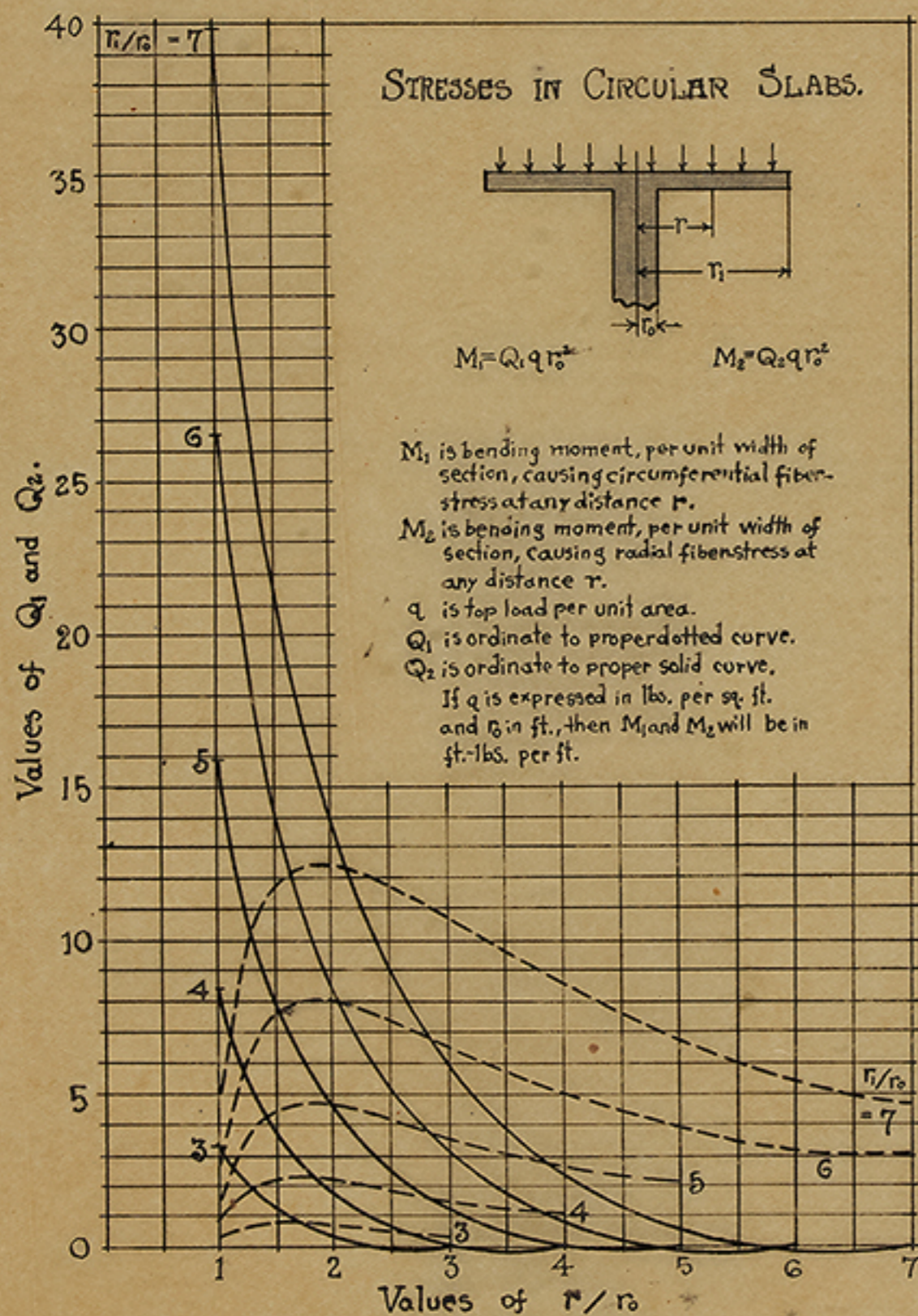


TABLE I	FORMULAE FOR RECTANGULAR BEAM.				
	r	$\frac{A_r}{bd}$	$\frac{m}{2t_1(t_1+m)}$	1	
t_1	$\frac{t}{c}$	$\frac{m}{2}(\sqrt{1+\frac{2}{mr}}-1)$		1'	
k	$k_1 d$	$\frac{m}{t_1+m} \cdot d$		2	
		$mr(\sqrt{1+\frac{2}{mr}}-1) \cdot d$		2'	
u	$u_1 d$	$\frac{k_1}{3} \cdot d$	$\frac{m}{3(t_1+m)} \cdot d$	3	
			$\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1) \cdot d$	3'	
j	$j_1 d$	$(1-u_1) \cdot d$	$(1-\frac{k_1}{3}) \cdot d$	4	
			$\frac{3t_1+2m}{3(t_1+m)} \cdot d$ $\{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)\} \cdot d$	4'	
A_r	rbd	$\frac{1}{j_1 t} \cdot \frac{M}{d}$	$\frac{1}{(1-\frac{k_1}{3}) \cdot t} \cdot \frac{M}{d}$	5	
			$\frac{1}{\{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)\} \cdot t} \cdot \frac{M}{d}$	5'	
		$\frac{1}{t_1 j_1 \cdot c} \cdot \frac{M}{d}$	$\frac{1}{t_1(1-\frac{k_1}{3}) \cdot c} \cdot \frac{M}{d}$	6	
			$\frac{1}{t_1 \{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)\} \cdot c} \cdot \frac{M}{d}$	6'	
d	$\sqrt{\frac{M}{N_1 b}}$	$\sqrt{\frac{1}{r j_1 \cdot t} \cdot \frac{M}{b}}$	$\sqrt{\frac{1}{r(1-\frac{k_1}{3}) \cdot t} \cdot \frac{M}{b}}$	7	
		$\sqrt{\frac{2}{k_1 j_1 \cdot c} \cdot \frac{M}{b}}$	$\sqrt{\frac{2}{k_1(1-\frac{k_1}{3}) \cdot c} \cdot \frac{M}{b}}$	8	
b	$\frac{M}{N_1 d^2}$	$\frac{1}{r j_1 \cdot t} \cdot \frac{M}{d^2}$	$\frac{1}{r(1-\frac{k_1}{3}) \cdot t} \cdot \frac{M}{d^2}$	9	
		$\frac{2}{k_1 j_1 \cdot c} \cdot \frac{M}{d^2}$	$\frac{2}{k_1(1-\frac{k_1}{3}) \cdot c} \cdot \frac{M}{d^2}$	10	
$(\frac{b}{a} \cdot \eta)$ d	$\sqrt[3]{\frac{M}{N_1 \eta}}$	$\sqrt[3]{\frac{1}{r j_1 \cdot t} \cdot \frac{M}{\eta}}$	$\sqrt[3]{\frac{1}{r(1-\frac{k_1}{3}) \cdot t} \cdot \frac{M}{\eta}}$	11	
		$\sqrt[3]{\frac{2}{k_1 j_1 \cdot c} \cdot \frac{M}{\eta}}$	$\sqrt[3]{\frac{2}{k_1(1-\frac{k_1}{3}) \cdot c} \cdot \frac{M}{\eta}}$	12	
t	$t_1 c$	$\frac{1}{r j_1} \cdot \frac{M}{bd^2}$	$\frac{1}{r(1-\frac{k_1}{3})} \cdot \frac{M}{bd^2}$	$\frac{3}{mr^2(2-\sqrt{1+\frac{2}{mr}})} \cdot \frac{M}{bd^2}$	13
c	$\frac{t}{t_1}$	$\frac{2}{k_1 j_1} \cdot \frac{M}{bd^2}$	$\frac{2}{k_1(1-\frac{k_1}{3})} \cdot \frac{M}{bd^2}$	$\frac{3(\sqrt{1+\frac{2}{mr}}-1)}{2r^2(2-\sqrt{1+\frac{2}{mr}})} \cdot \frac{M}{bd^2}$	14
$\frac{T}{C}$	$\frac{M}{j}$	$\frac{1}{j_1} \cdot \frac{M}{d}$	$\frac{1}{(1-\frac{k_1}{3})} \cdot \frac{M}{d}$	$\frac{3(t_1+m)}{3t_1+2m} \cdot \frac{M}{d}$	15
				$\frac{1}{1-\frac{mr}{3}(\sqrt{1+\frac{2}{mr}}-1)} \cdot \frac{M}{d}$	15'
M	T_j	$r j_1 \cdot t \cdot bd^2$	$r(1-\frac{k_1}{3}) \cdot t \cdot bd^2$	$\frac{3t_1+2m}{6t_1(t_1+m)^2} m \cdot t \cdot bd^2$	16
		C_j	$\frac{1}{2} k_1 j_1 \cdot c \cdot bd^2$	$\frac{k_1}{2} (1-\frac{k_1}{3}) \cdot c \cdot bd^2$	$\frac{3t_1+2m}{6(t_1+m)^2} m \cdot c \cdot bd^2$

a

b

The Beam and its Load with the B.M. and S.F. Diagrams.	B.M. Equation and Maximum B.M. M_x & M	Equation of Elastic Line, & Max. Deflection in Terms of The Loading. y or Δ .	Max. Deflection in Terms of Stress on Extreme Fiber of Symmetrical Section. Δ_f	Max. Stress on Extreme Fiber in Terms of the Loading Symmetrical Section. f .	Breaking weight in Terms of the fibre stress P	S.F. Equation, Max. S.F. and Reactions. S_x, S, R_a & R_b	Relative Strength
	$M_x = \frac{Pl}{30} (10 \frac{x^3}{l^3} - 9 \frac{x^2}{l^2} + 2)$ $M_a = -\frac{1}{15} Pl$ $M_b = -\frac{1}{10} Pl$ $M = \frac{3}{10} Pl - 0.429 Pl$ at $x = 1.17 \frac{l}{10} = 0.548 l$	$y = \frac{Pl^3}{60EI} (2 \frac{x^4}{l^4} - 5 \frac{x^3}{l^3} + \frac{x^2}{l^2})$ $\Delta = \frac{Pl^3}{384EI}$ for $x = 0.525 l$	$\Delta_f = \frac{10 fl^2}{192 Eh}$	$f = \frac{Plh}{20 I}$ $= \frac{Pl}{10 S_m}$	$P = \frac{20 fl}{lh}$ $= \frac{10 f S_m}{l}$	$S_x = \frac{1}{3} P - \frac{x^2}{l^2} P$ $S_b = -\frac{2}{3} P = R_b$ $S_a = \frac{1}{3} P = R_a$	$\frac{5}{4}$
	for $x < \frac{l}{2}$ $M_x = Px (\frac{1}{2} - \frac{x}{l})$ $M_{\frac{l}{2}} = \frac{Pl}{6}$	$y = \frac{Pl^3}{12EI} (\frac{5}{8} \frac{x^4}{l^4} - \frac{x^3}{l^3} + \frac{2}{3} \frac{x^2}{l^2})$ $\Delta = \frac{Pl^3}{60EI}$ at centre	$\Delta_f = \frac{1}{5} \frac{fl^2}{Eh}$	$f = \frac{Plh}{12 I}$ $= \frac{Pl}{6 S_m}$	$P = \frac{12 fl}{lh}$ $= \frac{6 f S_m}{l}$	for $x < \frac{l}{2}$ $S_x = P (\frac{1}{2} - \frac{x^2}{l^2})$ for $x > \frac{l}{2}$ $S_x = -P (\frac{1}{2} - \frac{2(1-x^2)}{l^2})$ $S_a = \frac{1}{2} P = R_a$ $S_b = -\frac{1}{2} P = R_b$	$\frac{3}{4}$
	for $x < \frac{l}{2}$ $M_x = -\frac{Pl}{48} (\frac{5x^3}{l^3} - \frac{x}{l})$ $M_a = M_b = -\frac{5}{48} Pl$ $M_c = \frac{Pl}{16}$	$y = \frac{Pl^3}{6EI} (\frac{5x^4}{16l^4} - \frac{x^2}{2l^2} + \frac{x^3}{5l^3})$ $\Delta = \frac{7Pl^3}{1920EI}$ at centre	$\Delta_f = \frac{7}{100} \frac{fl^2}{Eh}$	$f = \frac{5Plh}{96 I}$ $= \frac{5Pl}{48 S_m}$	$P = \frac{96 fl}{5lh}$ $= \frac{48 f S_m}{5l}$	for $x < \frac{l}{2}$ $S_x = P (\frac{1}{2} - \frac{2x^2}{l^2})$ $S_a = \frac{1}{2} P = R_a$ $S_b = \frac{1}{2} P = R_b$	$\frac{6}{5}$
	for $x < \frac{l}{2}$ $M_x = Px (\frac{1}{2} - \frac{x}{l} + \frac{2x^2}{3l^2})$ $M_c = \frac{Pl}{12}$	$y = \frac{Pl^3}{12EI} (\frac{3}{8} \frac{x^4}{l^4} - \frac{x^3}{l^3} + \frac{x^2}{l^2} - \frac{2}{5} \frac{x^3}{l^3})$ $\Delta = \frac{3}{320} \frac{Pl^3}{EI}$	$\Delta_f = \frac{9}{40} \frac{fl^2}{Eh}$	$f = \frac{Plh}{24 I}$ $= \frac{Pl}{12 S_m}$	$P = \frac{24 fl}{lh}$ $= \frac{12 f S_m}{l}$	for $x < \frac{l}{2}$ $S_x = \frac{2(\frac{1}{2} - x)^2}{l^2} P$ for $x > \frac{l}{2}$ $S_x = \frac{2(x - \frac{1}{2})^2}{l^2} P$ $S_a = \frac{1}{2} P = R_a$ $S_b = -\frac{1}{2} P = R_b$	$\frac{3}{2}$
	$M_x = \frac{x(1-x)}{6l} \{ R(2l-x) + P_1(l+x) \}$ $M = \frac{l^3}{7(R-P)} \{ (2P_1+P_2)(R-R)-(r^2+pr-2P_1^2) \}$ at $x = \frac{l}{3} \frac{r-P_1}{P_2-P_1}$ where $r = \sqrt{\frac{P_1^2+R^2+P_2^2}{3}}$					$S_x = R_a - \frac{M+Zx}{2}$ $S_a = \frac{1}{6} (2P_1+P_2) = R_a$ $S_b = -\frac{1}{6} (2P_2+R)$ where $Z = \frac{R_1}{P_1} + \frac{2(P_2-R)}{3}$	

DEPTH OF NEUTRAL AXIS
FOR VARIOUS RATIO OF STRESSES.

